

1. (12 pts.) Describe what each of the following symmetry operations are.

a. a  $C_3$  operation

1. \_\_\_\_\_

b. a  $\sigma_v$  operation

2. \_\_\_\_\_

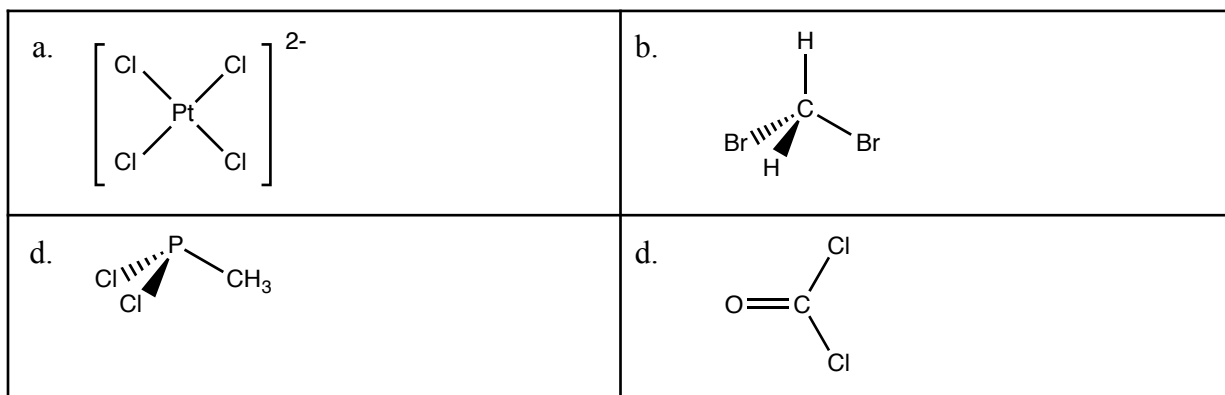
c. an  $S_4$  operation

3. \_\_\_\_\_

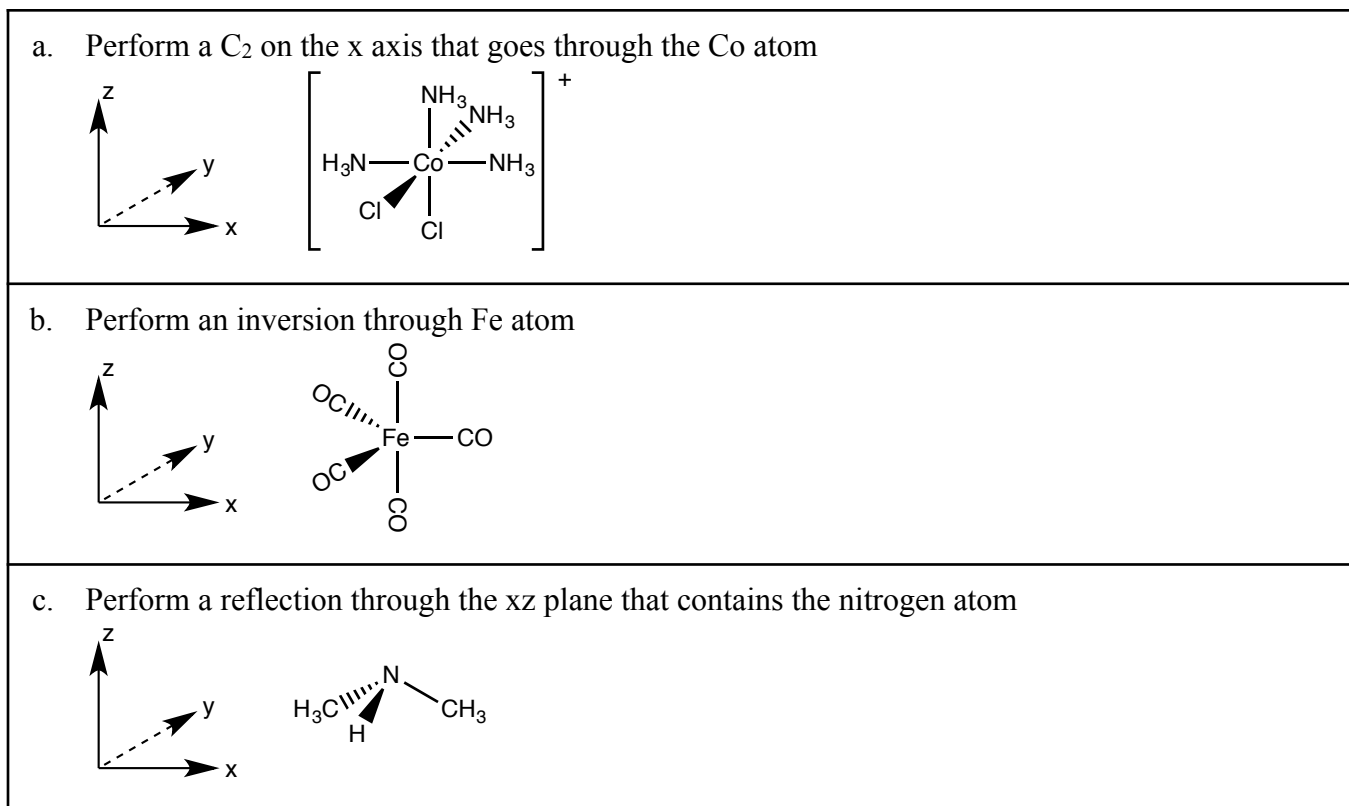
4. \_\_\_\_\_

5. \_\_\_\_\_

2. (16 pts.) Determine the point group for each of the following molecules. Wedge and dashed 3D representations have been provided.



3. (12 pts.) Perform the indicated operations on the following molecules, and draw a 3D representation, using wedge and dash notation where appropriate, for the resulting view.



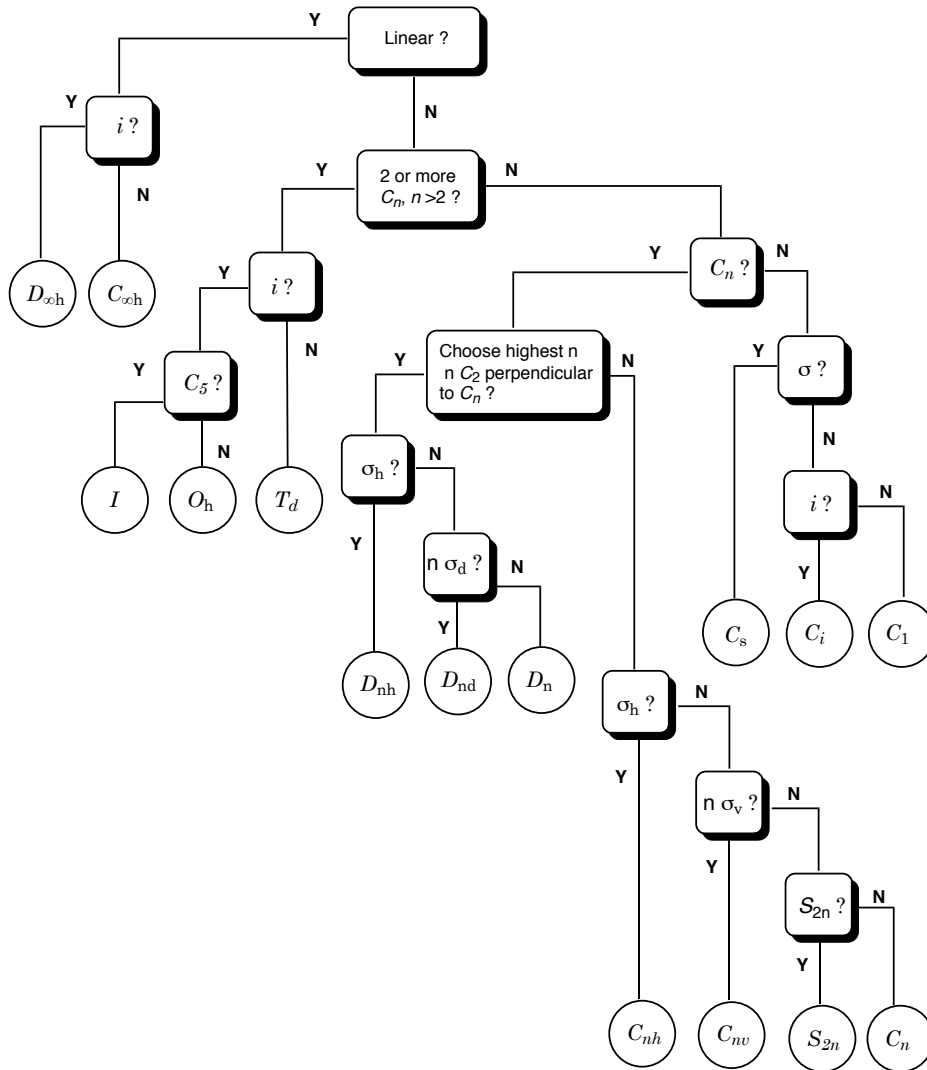
4. (10 pts.) Determine the irreducible representation for the reducible representation listed at the bottom of the following character table.

$T_d$	E	8 $C_3$	3 $C_2$	6 $S_4$	6 $\sigma_d$		
$A_1$	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_2$	1	1	1	-1	-1		
E	2	-1	2	0	0		$2z^2 - x^2 - y^2, x^2 - y^2$
$T_1$	3	0	-1	1	-1	$(R_x, R_y, R_z)$	
$T_2$	3	0	-1	-1	1	$(x, y, z)$	$(xy, xz, yz)$
$\Gamma$	6	3	2	-2	0		

5. (10 pt.) a. Determine the reducible representation for the C–Cl stretching vibrations for  $CH_2Cl_2$ .  
 b. Determine the irreducible representations for the C–Cl stretching vibrations.  
 c. Determine the number of C–Cl stretching bands that you would expect to see in the IR spectrum of  $CH_2Cl_2$ . The molecule is in the  $C_{2v}$  point group.

$C_{2v}$	E	$C_2$	$\sigma_v(xz)$	$\sigma_v(yz)$		
$A_1$	1	1	1	1	z	$x^2, y^2, z^2$
$A_2$	1	1	-1	-1	$R_z$	xy
$B_1$	1	-1	1	-1	x, $R_y$	xz
$B_2$	1	-1	-1	1	y, $R_x$	yz

### Point Group Assignment Tree



$$\left( \begin{array}{c} \text{number of irreducible} \\ \text{representations of a given} \\ \text{type needed} \end{array} \right) = \frac{1}{\text{order}} \sum_{\text{classes}} \left( \begin{array}{c} \# \text{ operations} \\ \text{in class} \end{array} \right) \left( \begin{array}{c} \chi \text{ of the irreducible} \\ \text{representation} \end{array} \right) \left( \begin{array}{c} \chi \text{ of the reducible} \\ \text{representation} \end{array} \right)$$